

Schwartz 2.2(a)

$$14 \text{ MeV} = 2 \gamma m c^2$$

$$m_{\text{proton}} \approx 938 \text{ MeV}/c^2$$

$$\frac{14 \text{ MeV}}{2 \times 938 \text{ MeV}} = 7.5 = \gamma = (1 - \beta^2)^{-1/2}$$

$$\Rightarrow \beta^2 \approx 0.982,$$

$$\beta \approx 0.99$$

$$(1 - 0.99) \times \frac{3 \times 10^8 \text{ m/s}}{10^3 \text{ m}} \times \frac{3600 \text{ s}}{1 \text{ hr}} \times 10^3 \text{ m}$$

$$= \frac{0.01 \times 3 \times 10^8 \times 3600}{10^3} \times \frac{10^3 \text{ m}}{\text{hr}}$$

$$= \boxed{10,800,000 \text{ km/hr}}$$

Davidson Cheng

3.6.2024

Schwartz 2.2(b)

In COM frame, we had

$p^0 = 2\gamma$, now we move to rest frame of one of the particles, we now have

$$p^0 = 1 + \gamma'$$

Equating them gives $2\gamma = 1 + \gamma'$, plugging $\gamma = 7.5$ from part (a), we have $\gamma' = 14$.

$$14 = \frac{1}{\sqrt{1-\beta^2}}$$

$$\beta \approx 0.997$$

Dawson Chew

3.6.2024